

# Mark Scheme (Results)

Summer 2012

GCE Core Mathematics C1 (6663) Paper 1





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## Summer 2012 6663 Core Mathematics C1 Mark Scheme

#### General Marking Guidance

- All candidates must receive the same treatment. Examiners must mark the first candidate in exactly the same way as they mark the last.
- Mark schemes should be applied positively. Candidates must be rewarded for what they have shown they can do rather than penalised for omissions.
- Examiners should mark according to the mark scheme not according to their perception of where the grade boundaries may lie.
- There is no ceiling on achievement. All marks on the mark scheme should be used appropriately.
- All the marks on the mark scheme are designed to be awarded. Examiners should always award full marks if deserved, i.e. if the answer matches the mark scheme. Examiners should also be prepared to award zero marks if the candidate's response is not worthy of credit according to the mark scheme.
- Where some judgement is required, mark schemes will provide the principles by which marks will be awarded and exemplification may be limited.
- When examiners are in doubt regarding the application of the mark scheme to a candidate's response, the team leader must be consulted.
- Crossed out work should be marked UNLESS the candidate has replaced it with an alternative response.

## EDEXCEL GCE MATHEMATICS

#### General Instructions for Marking

- 1. The total number of marks for the paper is 75.
- 2. The Edexcel Mathematics mark schemes use the following types of marks:
- M marks: method marks are awarded for 'knowing a method and attempting to apply it', unless otherwise indicated.
- A marks: Accuracy marks can only be awarded if the relevant method (M) marks have been earned.
- B marks are unconditional accuracy marks (independent of M marks)
- Marks should not be subdivided.
- 3. Abbreviations

These are some of the traditional marking abbreviations that will appear in the mark schemes and can be used if you are using the annotation facility on ePEN.

- bod benefit of doubt
- ft follow through
- the symbol / will be used for correct ft
- cao correct answer only
- cso correct solution only. There must be no errors in this part of the question to obtain this mark
- isw ignore subsequent working
- awrt answers which round to
- SC: special case
- oe or equivalent (and appropriate)
- dep dependent
- indep independent
- dp decimal places
- sf significant figures
- \* The answer is printed on the paper
- The second mark is dependent on gaining the first mark
- 4. All A marks are 'correct answer only' (cao.), unless shown, for example, as A1 ft to indicate that previous wrong working is to be followed through. After a misread however, the subsequent A marks affected are treated as A ft, but manifestly absurd answers should never be awarded A marks.

General Principles for Core Mathematics Marking

(But note that specific mark schemes may sometimes override these general principles).

Method mark for solving 3 term quadratic:

1. Factorisation

 $\frac{bnsatton}{(x^2 + bx + c)} = (x + p)(x + q), \text{ where } |pq| = |c|, \text{ leading to } x = \dots$  $(ax^2 + bx + c) = (mx + p)(nx + q), \text{ where } |pq| = |c| \text{ and } |mn| = |a|, \text{ leading to } x = \dots$ 

## 2. <u>Formula</u>

Attempt to use <u>correct</u> formula (with values for a, b and c), leading to  $x = \dots$ 

3. <u>Completing the square</u>

Solving  $x^2 + bx + c = 0$ :  $(x \pm \frac{b}{2})^2 \pm q \pm c, q \neq 0$ , leading to  $x = \dots$ 

Method marks for differentiation and integration:

## 1. Differentiation

Power of at least one term decreased by 1. ( $x^n \rightarrow x^{n-1}$ )

## 2. Integration

Power of at least one term increased by 1. ( $x^n \rightarrow x^{n+1}$ )

## Use of a formula

Where a method involves using a formula that has been learnt, the advice given in recent examiners' reports is that the formula should be quoted first.

Normal marking procedure is as follows:

<u>Method mark</u> for quoting a correct formula and attempting to use it, even if there are mistakes in the substitution of values.

Where the formula is <u>not</u> quoted, the method mark can be gained by implication from <u>correct</u> working with values, but may be lost if there is any mistake in the working.

## Exact answers

Examiners' reports have emphasised that where, for example, an <u>exact</u> answer is asked for, or working with surds is clearly required, marks will normally be lost if the candidate resorts to using rounded decimals.

## Answers without working

The rubric says that these <u>may</u> not gain full credit. Individual mark schemes will give details of what happens in particular cases. General policy is that if it could be done "in your head", detailed working would not be required.

## Summer 2012 6663 Core Mathematics C1 Mark Scheme

Question Number	Scheme	Marks	
1.	$\left\{ \int \left( 6x^2 + \frac{2}{x^2} + 5 \right) dx \right\} = \frac{6x^3}{3} + \frac{2x^{-1}}{-1} + 5x(+c)$	M1 A1	
	$= 2x^3 - 2x^{-1}; + 5x + c$	A1; A1	
		4	
	Notes		
	M1: for some attempt to integrate a term in x: $x^n \rightarrow x^{n+1}$		
	So seeing either $6x^2 \rightarrow \pm \lambda x^3$ or $\frac{2}{x^2} \rightarrow \pm \mu x^{-1}$ or $5 \rightarrow 5x$ is M1.		
	<b>1</b> <sup>st</sup> <b>A1</b> : for a correct un-simplified $x^3$ or $x^{-1}\left(\text{or } \frac{1}{x}\right)$ term.		
	<b>2<sup>nd</sup> A1:</b> for both $x^3$ and $x^{-1}$ terms correct and simplified on the same line. I.e. $2x^3 - 2x^{-1}$ or	$2x^3-\frac{2}{x}$ .	
	<b>3<sup>rd</sup> A1:</b> for $+5x + c$ . Also allow $+5x^{1} + c$ . This needs to be written on the same line.		
	Ignore the incorrect use of the integral sign in candidates' responses.		
	Ignore the metricet use of the meer of sign in continues responses.		
	<b>Note:</b> If a candidate scores M1A1A1A1 and their answer is NOT ON THE SAME LINE then final accuracy mark.	withhold the	

Question Number	Scheme	Mar	ks
<b>2.</b> (a)	$\left\{ (32)^{\frac{3}{5}} \right\} = \left(\sqrt[5]{32}\right)^3 \text{ or } \sqrt[5]{(32)^3} \text{ or } 2^3 \text{ or } \sqrt[5]{32768}$ $= 8$	M1	
	= 8	A1	
			[2]
(b)	$\left\{ \left(\frac{25x^4}{4}\right)^{-\frac{1}{2}} \right\} = \left(\frac{4}{25x^4}\right)^{\frac{1}{2}} \text{ or } \left(\frac{5x^2}{2}\right)^{-1} \text{ or } \frac{1}{\left(\frac{25x^4}{4}\right)^{\frac{1}{2}}}$ See notes below	M1	
	$= \frac{2}{5x^2} \text{ or } \frac{2}{5}x^{-2}$ See notes for other alternatives	A1	
	5, 5		[2]
	Notes		4
(a)	<b>M1</b> : for a full correct interpretation of the fractional power. Note: $5 \times (32)^3$ is M0.		
	A1: for 8 only. Note: Award M1A1 for writing down 8.		
(b)	<b>M1:</b> For use of $\frac{1}{2}$ OR use of $-1$		
	Use of $\frac{1}{2}$ : Candidate needs to demonstrate the they have rooted all three elements in their bracket.		
	<b>Use of -1:</b> Either Candidate has $\frac{1}{\text{Bracket}}$ or $\left(\frac{Ax^{C}}{B}\right)$ becomes $\left(\frac{B}{Ax^{C}}\right)$ .		
	Allow M1 for		
	• $\left(\frac{4}{25x^4}\right)^{\frac{1}{2}}$ or $\left(\frac{5x^2}{2}\right)^{-1}$ or $\frac{1}{\left(\frac{25x^4}{4}\right)^{\frac{1}{2}}}$ or $\sqrt{\left(\frac{4}{25x^4}\right)}$ or $\frac{1}{\sqrt{\left(\frac{25x^4}{4}\right)}}$ or $\left(\frac{\frac{1}{25x^4}}{\frac{1}{4}}\right)^{\frac{1}{2}}$ or $\frac{\frac{1}{5x^2}}{\frac{1}{2}}$	or $\frac{\frac{1}{5}x}{\frac{1}{2}}$	2
	or $-\left(\frac{5x^2}{2}\right)$ or $\left(\frac{-5x^{-2}}{-2}\right)$ or $-\left(\frac{5x^{-2}}{2}\right)$ or $\frac{5x^{-2}}{2}$		
	• $\left(\frac{4}{25x^4}\right)^K$ or $\left(\frac{5x^2}{2}\right)^C$ where <i>K</i> , <i>C</i> are any powers including 1.		
	A1: for either $\frac{2}{5x^2}$ or $\frac{2}{5}x^{-2}$ or $0.4x^{-2}$ or $\frac{0.4}{x^2}$ .		
	Note: $\left(\sqrt{\left(\frac{25x^4}{4}\right)}\right)^{-1}$ is not enough work by itself for the method mark.		
	Note: A final answer of $\frac{1}{\frac{5}{2}x^2}$ or $\frac{1}{2\frac{1}{2}x^2}$ or $\frac{1}{2.5x^2}$ is A0.		
	Note: Also allow $\pm \frac{2}{5x^2}$ or $\pm \frac{2}{5}x^{-2}$ or $\pm 0.4x^{-2}$ or $\pm \frac{0.4}{x^2}$ for A1.		

Question Number	Scheme		Marks	
3.	$\left\{\frac{2}{\sqrt{12}-\sqrt{8}}\right\} = \frac{2}{\left(\sqrt{12}-\sqrt{8}\right)} \times \frac{\left(\sqrt{12}+\sqrt{8}\right)}{\left(\sqrt{12}+\sqrt{8}\right)}$ Writing this is sufficient	nt for M1.	M1	
	$= \frac{1}{12-8}$ This mark can be	or 12 – 8. e implied.	A1	
	$= \frac{2(2\sqrt{3}+2\sqrt{2})}{12-8}$		B1 B1	
	$= \sqrt{3} + \sqrt{2}$		A1 cso	5
	Notes			
	M1: for a correct method to rationalise the denominator.	· · · ·		
	<b>1</b> <sup>st</sup> <b>A1:</b> $(\sqrt{12} - \sqrt{8})(\sqrt{12} + \sqrt{8}) \to 12 - 8$ or $(\sqrt{3} + \sqrt{2})(\sqrt{3} - \sqrt{2}) \to 3 - \sqrt{2}$	- 2		
	<b>1</b> <sup>st</sup> <b>B1:</b> for $\sqrt{12} = 2\sqrt{3}$ or $\sqrt{48} = 4\sqrt{3}$ seen or implied in candidate's working.			
	<b>2<sup>nd</sup> B1:</b> for $\sqrt{8} = 2\sqrt{2}$ or $\sqrt{32} = 4\sqrt{2}$ seen or implied in candidate's working.			
	<b>2<sup>nd</sup> A1:</b> for $\sqrt{3} + \sqrt{2}$ . Note: $\frac{\sqrt{3} + \sqrt{2}}{1}$ as a final answer is A0.			
	Note: The first accuracy mark is dependent on the first method mark being awarded			
	Note: $\frac{1}{2}\sqrt{12} + \frac{1}{2}\sqrt{8} = \sqrt{3} + \sqrt{2}$ with no intermediate working implies the B1B1 ma			
	Note: $\sqrt{12} = \sqrt{4}\sqrt{3}$ or $\sqrt{8} = \sqrt{4}\sqrt{2}$ are not sufficient for the B1 marks.			
	<b>Note:</b> A candidate who writes down (by misread) $\sqrt{18}$ for $\sqrt{8}$ can potentially obtain M1A0B1B			ere
	the 2 <sup>nd</sup> B1 will be awarded for $\sqrt{18} = 3\sqrt{2}$ or $\sqrt{72} = 6\sqrt{2}$			
	<b>Note:</b> The final accuracy mark is for a correct solution only. <u>Alternative 1 solution</u>			
	$\left\{\frac{2}{\sqrt{12} - \sqrt{8}}\right\} = \frac{2}{\left(2\sqrt{3} - 2\sqrt{2}\right)}$ B1 B1			
	$= \frac{1}{(\sqrt{3} - \sqrt{2})} \times \frac{(\sqrt{3} + \sqrt{2})}{(\sqrt{3} + \sqrt{2})} $ M1	Please reco marks in tl places on t mark grid.	he relevant he	
	$= \frac{\left\{ \left( \sqrt{3} + \sqrt{2} \right) \right\}}{3 - 2}$ A1 for 3 - 2	illai k gi lu.		
	$= \sqrt{3} + \sqrt{2} $ A1			
	Alternative 2 solution			
	$\left\{\frac{2}{\sqrt{12}-\sqrt{8}}\right\} = \frac{2}{\left(2\sqrt{3}-2\sqrt{2}\right)} = \frac{1}{\left(\sqrt{3}-\sqrt{2}\right)} = \sqrt{3}+\sqrt{2} , \text{ or } \frac{2}{\left(2\sqrt{3}-2\sqrt{2}\right)}$	$\overline{\overline{2}} = \sqrt{3} +$	$+\sqrt{2}$	
	with no incorrect working seen is awarded M1A1B1B1A1.			

Question Number	Scheme	Marks
<b>4.</b> (a)	$y = 5x^{3} - 6x^{\frac{4}{3}} + 2x - 3$ $\left\{\frac{dy}{dx} = \right\}  5(3)x^{2} - 6\left(\frac{4}{3}\right)x^{\frac{1}{3}} + 2$	M1
	$= 15x^2 - 8x^{\frac{1}{3}} + 2$	A1 A1 A1
(b)	$\left\{\frac{d^2 y}{dx^2} = \right\} 30x - \frac{8}{3}x^{-\frac{2}{3}}$	[4] M1 A1
		[2] 6
	Notes	
(-)	M1: for an attempt to differentiate $x^n \rightarrow x^{n-1}$ to one of the first three terms of $y = 5x^3 - 6$ .	$x^{\frac{4}{3}} + 2x - 3$ .
(a)	So seeing either $5x^3 \rightarrow \pm \lambda x^2$ or $-6x^{\frac{4}{3}} \rightarrow \pm \mu x^{\frac{1}{3}}$ or $2x \rightarrow 2$ is M1. <b>1</b> <sup>st</sup> A1: for $15x^2$ only.	
	<b>2<sup>nd</sup> A1:</b> for $-8x^{\frac{1}{3}}$ or $-8\sqrt[3]{x}$ only.	
	<b>3</b> <sup>rd</sup> A1: for $+2$ (+ <i>c</i> included in part (a) loses this mark). Note: $2x^0$ is A0 unless simplified	to 2.
(b)	M1: For differentiating $\frac{dy}{dx}$ again to give either • a correct follow through differentiation of their $x^2$ term • or for $\pm \alpha x^{\frac{1}{3}} \rightarrow \pm \beta x^{-\frac{2}{3}}$ . A1: for any <i>correct</i> expression <i>on the same line</i> (accept un-simplified coefficients).	
	For powers: $30x^{2-1} - \frac{8}{3}x^{\frac{1}{3}-1}$ is A0, but writing powers as one term eg: $(15 \times 2x) - \frac{8}{3}x^{-\frac{4}{6}}$ is a	ok for A1.
	Note: Candidates leaving their answers as $\left\{\frac{dy}{dx}=\right\}15x^2-\frac{24}{3}x^{\frac{1}{3}}+2$ and $\left(\frac{d^2y}{dx^2}=\right)30x-\frac{24}{3}x^{\frac{1}{3}}+2$	$\frac{4}{9}x^{-\frac{2}{3}}$ are
	awarded M1A1A0A1 in part (a) and M1A1 in part (b).	
	<b>Be careful:</b> $30x - \frac{8}{3}x^{-\frac{1}{3}}$ will be A0.	
	Note: For an extra term appearing in part (b) on the same line, ie $30x - \frac{8}{3}x^{-\frac{2}{3}} + 2$ is M1A0	
	Note: If a candidate writes in part (a) $15x^2 - 8x^{\frac{1}{3}} + 2 + c$ and in part (b) $30x - \frac{8}{3}x^{-\frac{2}{3}} + c$	
	then award (a) M1A1A1A0 (b) M1A1	

Question Number	Scheme	Marks
	$a_1 = 3, a_{n+1} = 2a_n - c, n \ge 1, c \text{ is a constant}$	
<b>5.</b> (a)	$\{a_2 =\} 2 \times 3 - c \text{ or } 2(3) - c \text{ or } 6 - c$	B1
(b)	$ \{a_3 =\} 2 \times ("6 - c") - c = 12 - 3c (*) $	[1] M1 A1 cso
(c)	$a_4 = 2 \times ("12 - 3c") - c \qquad \{= 24 - 7c\}$	[2] M1
	$\left\{\sum_{i=1}^{4} a_i = \right\}  3 + (6 - c) + (12 - 3c) + (24 - 7c)$	M1
	$"45 - 11c" \ge 23$ or $"45 - 11c" = 23$	M1
	$c \le 2 \text{ or } 2 \ge c$	A1 cso [4]
	Notes	/
(a) (b) (c)	The answer to part (a) cannot be recovered from candidate's working in part (b) or part (c). Once the candidate has achieved the correct result you can ignore subsequent working in this part M1: For a correct substitution of <i>their</i> $a_2$ <i>which must include term(s) in c</i> into $2a_2 - c$ giving $a_3$ in terms of only c. Candidates must use correct bracketing for this mark. A1: for correct solution only. No incorrect working/statements seen. (Note: the answer is given $1^{st}$ M1: For a correct substitution of $a_3$ which must include term(s) in c into $2a_3 - c$ giving a in terms of only c. Candidates must use correct bracketing (can be implied) for this mark. $2^{nd}$ M1: for an attempt to sum their $a_1$ , $a_2$ , $a_3$ and $a_4$ only. $3^{rd}$ M1: for their sum (of 3 or 4 or 5 consecutive terms) = or $\geq$ or > 23 to form a linear inequality.	g a result for ven!) result for $a_4$
	equation in c. A1: for $c \le 2$ or $2 \ge c$ from a correct solution only.	uanty of
	<b>Beware:</b> $-11c \ge -22 \implies c \ge 2$ is A0. <b>Note:</b> $45 - 11c \ge 23 \implies -11c \le -22 \implies c \le 2$ would be A0 cso.	
	Note: Applying either $S_n = \frac{n}{2} (2a + (n-1)d)$ or $S_n = \frac{n}{2} (a+l)$ is $2^{nd}$ M0, $3^{rd}$ M0.	
	<b>Note:</b> If a candidate gives a numerical answer in part (a); they will then get M0A0 in part (b); the printed result of $a_3 = 12 - 3c$ they could potentially get M0M1M1A0 in part (c) <b>Note:</b> If a candidate only adds numerical values (not in terms of c) in part (c) then they could pointly M0M0M1A0. <b>Note:</b> For the 3 <sup>rd</sup> M1 candidates will usually sum $a_1$ , $a_2$ , $a_3$ and $a_4$ or $a_2$ , $a_3$ and $a_4$ or $a_2$ ,	potentially get
	or $a_1, a_2, a_3, a_4$ and $a_5$	

Number	Scheme	Mark	S
	Boy's Sequence: 10, 15, 20, 25,		
<b>6.</b> (a)	$\{a = 10, d = 5 \Rightarrow T_{15} =\} a + 14d = 10 + 14(5); = 80 \text{ or } 0.1 + 14(0.05); = \text{\pounds}0.80$	M1; A1	[2]
(b)	$\left\{S_{60} = \right\} \frac{60}{2} \left[2(10) + 59(5)\right]$	M1 A1	
	= 30(315) = 9450 or £94.50	A1	
	Boy's Sister's Sequence: 10, 20, 30, 40,		[3]
(c)	$\{a = 10, d = 10 \Rightarrow S_m =\} \frac{m}{2} (2(10) + (m-1)(10))  \left(\text{or } \frac{m}{2} \times 10(m+1) \text{ or } 5m(m+1)\right)$	M1 A1	
	63 or 6300 = $\frac{m}{2} (2(10) + (m-1)(10))$	dM1	
	$6300 = \frac{m}{2}(10)(m+1)  \text{or}  12600 = 10m(m+1)$		
	1260 = m(m+1)		
	$35 \times 36 = m(m+1)$ (*)	A1 cso	[4]
(d)	${m =} 35$	B1	[4]
			[1] 10
	Notes		10
(a)	M1: for using the formula $a + 14d$ with either a or d correct.		
	A1: for 80 or 80p or £0.80 or £0.80p and apply ISW. Otherwise, £80 or 0.80 or 0.80p would	d be A0.	
	Award M0 if candidate applies $a + 59d$ .		
	Listing the first 15 terms and highlighting that the 15 <sup>th</sup> term is 80 or listing 15 terms with the finaligned with 80 will then be awarded all two marks of M1A1. Writing down 80 with no working is M1A1.	nal 15 <sup>th</sup> teri	m
(b)	<b>M1</b> : for use of correct $\frac{60}{2} [2(10) + 59(5)]$ or $\frac{15}{2} (2(10) + 14(5))$		
	with $a = 10$ , $d = 5$ and $n = 60$ or $a = 10$ , $d = 5$ and $n = 15$ .		
	If a candidate uses $\frac{n}{2}(a+l)$ with $n = 60$ or 15, there must be a full method of finding or statin	g <i>l</i> as eithe	er
	a + 59d (= 305) or $a + 14d (= 80)$ , respectively.		
	<b>1</b> <sup>st</sup> <b>A1:</b> for a correct expression for $S_{60}$ . ie. $\frac{60}{2} [2(10) + 59(5)]$ or $\frac{60}{2} [2(0.1) + 59(0.05)]$		
	or $\frac{60}{2} [10 + 305]$ or $\frac{60}{2} [0.10 + 3.05]$ . This mark can be implied by later working.		
	$2^{nd}$ A1: for 9450 or 9450p or £94.50 and apply ISW. Otherwise, £9450 or 94.50 without 60	t£sign is A	<b>A</b> 0.
	<b>Note</b> : the bracketing error of $\frac{60}{2}$ 2(10) + 59(5) is A0 unless recovered from later working.		
	Adding together the first 60 terms to obtain 9450 will then be awarded all three marks of M1A	1A1.	

1<sup>st</sup> M1: for correct use of  $S_m$  formula with one of a or d correct. (c) **1**<sup>st</sup> **A1:** for a correct expression for  $S_m$ . Eg:  $\frac{m}{2}(2(10) + (m-1)(10))$  or  $\frac{m}{2} \times 10(m+1)$  or 5m(m+1) $2^{nd}$  M1: for forming a suitable equation using 63 or 6300 and their  $S_m$ . Dependent on  $1^{st}$  M1. 2<sup>nd</sup> A1cso: for *reaching the printed result* with no incorrect working seen. Long multiplication is not necessary for the final accuracy mark. Note:  $\frac{m}{2}(2(10) + (m-1)(10)) = 630$  and not either 6300 or 63 is dM0. Beware: Some candidates will try and fudge the result given on the question paper. Notes for awarding 2<sup>nd</sup> A1 Going from m(m+1) = 1260 straight to  $m(m+1) = 35 \times 36$  is  $2^{nd}$  A1. Going from m(m+1) = some factor decomposition of 6300 straight to  $m(m+1) = 35 \times 36$  is  $2^{nd}$  A1. Going from 10m(m+1) = 12600 straight to  $m(m+1) = 35 \times 36$  is  $2^{nd}$  A0. Going from  $m(m+1) = \frac{6300}{5}$  straight to  $m(m+1) = 35 \times 36$  is 2<sup>nd</sup> A0. Alternative: working in an different letter, say n or p. **M1A1:** for  $\frac{n}{2}(2(10) + (n-1)(10))$  (although mixing letters eg.  $\frac{n}{2}(2(10) + (m-1)(10))$  is M0A0). **dM1:** for 63 or 6300 =  $\frac{n}{2}(2(10) + (n-1)(10))$ Leading to  $6300 = \frac{n}{2}(10)(n+1) \implies 1260 = n(n+1) \implies 35 \times 36 = n(n+1)$ The candidate then needs to write either  $35 \times 36 = m(m+1)$  or  $m \equiv n$  or m = n to gain the final A1. (d) **B1:** for 35 only.

Question Number	Scheme	Marks
	$P(4, -1)$ lies on C where $f'(x) = \frac{1}{2}x - \frac{6}{\sqrt{x}} + 3, x > 0$	
<b>7.</b> (a)	$f'(4) = \frac{1}{2}(4) - \frac{6}{\sqrt{4}} + 3; = 2$	M1; A1
	<b>T:</b> $y - 1 = 2(x - 4)$	dM1
	<b>T:</b> $y = 2x - 9$	A1 [4]
(b)	$f(x) = \frac{x^{1+1}}{2(2)} - \frac{6x^{-\frac{1}{2}+1}}{(\frac{1}{2})} + 3x(+c)$ or equivalent.	M1 A1
	${f(4) = -1 \Rightarrow} \frac{16}{4} - 12(2) + 3(4) + c = -1$	dM1
	$\left\{4-24+12+c=-1 \implies c=7\right\}$	
	So, $\{f(x) =\} \frac{x^2}{2(2)} - \frac{6x^{\frac{1}{2}}}{(\frac{1}{2})} + 3x + 7$	A1 cso
	$\left\{ \text{NB: } f(x) = \frac{x^2}{4} - 12\sqrt{x} + 3x + 7 \right\}$	[4]
		8
	Notes	
(a)	<b>1<sup>st</sup> M1:</b> for clear attempt at $f'(4)$ .	
	<b>1<sup>st</sup> A1:</b> for obtaining 2 from $f'(4)$ .	
	<b>2<sup>nd</sup> dM1:</b> for $y - 1 = (\text{their } f'(4))(x - 4)$ or $\frac{y - 1}{x - 4} = (\text{their } f'(4))$	
	or full method of $y = mx + c$ , with $x = 4$ , $y = -1$ and their f'(4) to find a value f <b>Note:</b> this method mark is dependent on the first method mark being awarded. <b>2<sup>nd</sup> A1:</b> for $y = 2x - 9$ or $y = -9 + 2x$	or <i>c</i> .
(b)	Note: This work needs to be contained in part (a) only. 1 <sup>st</sup> M1: for a clear attempt to integrate $f'(x)$ with at least one correct application of	
	$x^n \to x^{n+1}$ on $f'(x) = \frac{1}{2}x - \frac{6}{\sqrt{x}} + 3$ .	
	So seeing either $\frac{1}{2}x \rightarrow \pm \lambda x^{1+1}$ or $-\frac{6}{\sqrt{x}} \rightarrow \pm \mu x^{-\frac{1}{2}+1}$ or $3 \rightarrow 3x^{0+1}$ is M1.	
	1 <sup>st</sup> A1: for correct un-simplified coefficients and powers (or equivalent) with or without $+c$ .	
	<b>2<sup>nd</sup> dM1:</b> for use of $x = 4$ and $y = -1$ in an integrated equation to form a linear equation in c	
	ie: applying $f(4) = -1$ . This mark is dependent on the first method mark being away	arded.
	$r^{2} = 6r^{\frac{1}{2}}$	
	A1: For $\{f(x)=\}\frac{x^2}{2(2)} - \frac{6x^{\frac{1}{2}}}{(\frac{1}{2})} + 3x + 7$ stated on one line where coefficients can be un-stated on the state of the stat	simplified or
	simplified, but must contain one term powers. Note this mark is for correct solution	n only.
	Note: For a candidate attempting to find $f(x)$ in part (a) If it is clear that they understand that they are finding $f(x)$ in part (a); is by writing $f(x) = -\infty$	ry - than
	If it is clear that they understand that they are finding $f(x)$ in part (a); ie. by writing $f(x) =$ o you can give credit for this working in part (b).	$y = \dots$ then
	you can give creat for any working in part (0).	

Question Number	Scheme	Marks
	$4x - 5 - x^2 = q - (x - p)^2$ , p, q are integers.	
<b>8.</b> (a)	$\left\{4x - 5 - x^2\right\} - \left[x^2 - 4x + 5\right] = -\left[(x - 2)^2 - 4 + 5\right] = -\left[(x - 2)^2 + 1\right]$	M1
	$= -1 - (x - 2)^2$	A1 A1 [ <b>3</b> ]
(b)	$\{"b^2 - 4ac" = \} 4^2 - 4(-1)(-5) = \{= 16 - 20\}$	[3] M1
	= - 4	A1
(c)	<i>y</i> <b>▲</b>	[2]
	$\begin{array}{c c} O \\ \hline \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\$	M1
	- 5 Maximum <b>within</b> the 4 <sup>th</sup> quadrant	A1
	Curve cuts through -5 or $(0, -5)$ marked on the y-axis	B1
		[3]
		8
	<b>Notes</b> M1: for an attempt to complete the square eg: $\pm (\pm x \pm 2)^2 \pm k - 5$ , $k \neq 0$ or $\pm (\pm x \pm 2)^2 \pm k - 5$	2 2 4 5
(a)	M1: for an attempt to complete the square eg: $\pm (\pm x \pm 2)^2 \pm k - 5$ , $k \neq 0$ or $\pm (\pm x \pm 2)^2 \pm$ seen or implied in working.	$\lambda, \lambda \neq -3$
	1 <sup>st</sup> A1: for $p = -2$ or for $\pm \alpha - (x-2)^2$ , $\alpha$ can be 0. 2 <sup>nd</sup> A1: for $q = -1$	
	<b>2</b> A1: for $q = -1$ Note: Allow M1A1A1 for a correct written down expression of $-1 - (x - 2)^2$ Ignore $-1 - (x - 2)^2$	$(2)^2 = 0$
	Note: If a candidate states either $p = -2$ or $q = -1$ or writes $\pm k - (x - 2)^2$ then imply the M1 in Note: A candidate who writes down with no working $p = 2$ , $q = (a \text{ value which is not } -1)$ gets N	
	Note: Writing $(x-2)^2 - 1$ , followed by $p = -2$ , $q = -1$ is M1A1A0.	
	Alternative 1 to (a)	
	$\frac{4x - 5 - x^2}{4x - 5 - x^2} = \frac{1}{2} - $	
	<u>Alternative2 to (a)</u>	
	$q - (x + p)^2 = q - (x^2 + 2px + p^2) = -x^2 - 2px + q - p^2$ Compare x terms: $-2p = 4 \implies p = -2$	
	Compare constant terms: $2p^{-1} \Rightarrow \frac{p^{-2}}{p} = -5 \Rightarrow q - 4 = -5 \Rightarrow q = -1$	
	<b>M1:</b> Either $\pm 2p = 4$ or $q \pm p^2 = -5$ ; <b>1<sup>st</sup> A1:</b> for $p = -2$ ; <b>2<sup>nd</sup> A1:</b> for $q = -1$	

	$\frac{Alternative 3 to (a)}{\text{Negating } 4x - 5 - x^2 \text{ gives } x^2 - 4x + 5}$
	So, $x^2 - 4x + 5 = (x - 2)^2 - 4 + 5 \{= (x - 2)^2 + 1\}$ M1 for $\pm (\pm x \pm 2)^2 \pm k + 5$
	then stating $p = -2$ is $1^{st} A1$ and/or $q = -1$ is $2^{nd} A1$ .
	or writing $-1 - (x - 2)^2$ is A1A1.
	Special Case for part (a):
	$q - (x + p)^{2} = q - (x^{2} + 2px + p^{2}) = -x^{2} - 2px + q - p^{2} = 4x - 5 - x^{2}$
	$\Rightarrow -2px + q - p^2 = 4x - 5 \Rightarrow q - p^2 + 5 = 4x + 2px \Rightarrow q - p^2 + 5 = x(4 + 2p)$
	$\Rightarrow x = \frac{q - p^2 + 5}{4 + 2p} \Rightarrow p \neq -2 \text{ scores Special Case M1A1A1 only once } p \neq -2 \text{ achieved.}$
(b)	M1: for correctly substituting any two of $a = -1$ , $b = 4$ , $c = -5$ into $b^2 - 4ac$ if this is quoted.
	If $b^2 - 4ac$ is not quoted then the substitution must be correct.
	Substitution into $b^2 < 4ac$ or $b^2 = 4ac$ or $b^2 > 4ac$ is M0.
	A1: for $-4$ only.
	If they write $-4 < 0$ treat the $< 0$ as ISW and award A1. If they write $-4 \ge 0$ then score A0.
	So substituting into $b^2 - 4ac < 0$ leading to $-4 < 0$ can score M1A1
	Note: Only award marks for use of the discriminant in part (b).
	Note: Award M0 if the candidate uses the quadratic formula UNLESS they later go on to identify that the
	discriminant is the result of $b^2 - 4ac$ .
	Beware: A number of candidates are writing up their solution to part (b) at the bottom of the second page. So please look!
(c)	<b>M1:</b> Correct $\cap$ shape in any quadrant.
	A1: The maximum must be <i>within</i> the fourth quadrant to award this mark.
	<b>B1:</b> Curve ( <i>and not line!</i> ) cuts through -5 or $(0, -5)$ marked on the y-axis
	Allow $(-5, 0)$ rather than $(0, -5)$ if marked in the "correct" place on the <i>y</i> -axis.
	If the curve cuts through the negative y-axis and this is not marked, then you can recover $(0, -5)$ from the
	candidate's working in part (c). You are not allowed to recover this point, though, from a table of values.
	Note: Do not recover work for part (a) in part (c).

Question Number	Scheme	Marks
Trumber	$L_1: 4y + 3 = 2x \implies y = \frac{1}{2}x - \frac{3}{4}; A(p, 4) \text{ lies on } L_1.$	
<b>9.</b> (a)	${p = 9\frac{1}{2} \text{ or } \frac{19}{2} \text{ or } 9.5}$	B1
	(1, 2, 2) $2x-3$ $(1, 2)$	[1]
(b)	$\{4y + 3 = 2x\} \Rightarrow y = \frac{2x - 3}{4} \Rightarrow m(L_1) = \frac{1}{2} \text{ or } \frac{2}{4}$	M1 A1
	So $m(L_2) = -2$ $L_2$ : $y - 4 = -2(x - 2)$	B1ft M1
	$L_2: 2x + y - 8 = 0$ or $L_2: 2x + 1y - 8 = 0$	A1
	1 2	[5]
(c)	$\{L_1 = L_2 \Rightarrow\}$ 4(8-2x) + 3 = 2x or -2x + 8 = $\frac{1}{2}x - \frac{3}{4}$	M1
	x = 3.5, y = 1	A1, A1 cso [ <b>3</b> ]
(d)	$CD^{2} = ("3.5" - 2)^{2} + ("1" - 4)^{2}$	"M1"
	$CD = \sqrt{\left("3.5" - 2\right)^2 + \left("1" - 4\right)^2}$	A1 ft
	$=\sqrt{1.5^2+3^2}=1.5\sqrt{1^2+2^2}=1.5\sqrt{5}$ or $\frac{3}{2}\sqrt{5}$ (*)	A1 cso
	$A_{rea} = triangle ABC + triangle ABE$	[3]
(e)	Area = triangle ABC + triangle ABE = $\frac{1}{2} \times \frac{3}{2}\sqrt{5} \times \sqrt{80} + \frac{1}{2} \times 3\sqrt{5} \times \sqrt{80}$ Finding the area of any triangle.	M1
	$=\frac{3}{4}\sqrt{5} \times 4\sqrt{5} + \frac{3}{2}\sqrt{5} \times 4\sqrt{5}$	
	$=\frac{3}{4}(20) + \frac{3}{2}(20)$	B1
	4 2 = 45	A1
		[3] 15
	Notes	13
<b>9.</b> (a) (b)	<b>B1:</b> 9.5 oe. 1 <sup>st</sup> M1: for an attempt to rearrange $4y + 3 = 2x$ into $y = mx + c$ .	
(-)	This mark can be implied by the correct gradient of $L_1$ or $L_2$ .	
	1 <sup>st</sup> A1: for gradient of $L_1 = \frac{1}{2}$ or $\frac{2}{4}$ . Stating $m(L_1) = \frac{1}{2}$ without working is M1A1.	
	<b>B1ft:</b> for applying $m(L_2) = \frac{-1}{\text{their } m(L_1)}$ . Need not be simplified.	
	Note: Writing down $m(L_2) = -2$ with <i>no earlier incorrect working</i> gains M1A1B1	
	<b>2<sup>nd</sup> M1:</b> for applying $y - 4 = \pm \lambda(x - 2)$ where $\lambda$ is a numerical value, $\lambda \neq 0$ . or full method of $y = mx + c$ , with $x = 2$ , $y = 4$ and (their $\pm \lambda$ ) to find c.	
	<b>2<sup>nd</sup> A1:</b> $2x + y - 8 = 0$ or $-2x - y + 8 = 0$ or $y + 2x - 8 = 0$ or $4x + 2y - 16 = 0$	
	or $2x + 1y - 8 = 0$ etc. Must be "= 0". So do not allow $2x + y = 8$ etc.	
	<b>Note:</b> Condone the error of incorrectly rearranging $L_1$ to give $y = \frac{1}{2}x - 3 \Rightarrow m(L_1) = \frac{1}{2}$ .	

(c)	M1: for an attempt to solve. Must form a linear equation in one variable. $1^{st}$ A1: for $x = 3.5$ (correct solution only).
	<b><math>2^{nd}</math> A1:</b> for $y = 1$ (correct solution only).
	Note: If $x = 3.5$ , $y = 1$ is found from no working, then send to review.
	<b>Note:</b> Use of trial and error to find one of x or y and then substitution into one of $L_1$ or $L_2$ can achieve
	M1A1A1.
(d)	M1: for an attempt at $CD^2$ - ft their point D. Eg: $("3.5"-2)^2 + ("1"-4)^2$ or simplified.
	This mark can be implied by finding <i>CD</i> .
	<b>1</b> <sup>st</sup> <b>A1ft:</b> for finding their <i>CD</i> - ft their point <i>D</i> . Eg: $\sqrt{("3.5"-2)^2 + ("1"-4)^2}$ or correctly simplified.
	<b>1</b> Aft. For many then $CD$ - it then point $D$ . Eg. $\sqrt{(3.3 - 2)} + (1 - 4)$ of concerning simplified. <b>2<sup>nd</sup> A1:cso</b> for no incorrect working seen.
	Note: A candidate initially writing down $\sqrt{1.5^2 + 3^2}$ can be awarded M1A1.
	<u>Alternatives part (d): Final accuracy</u> <b>1.</b> $\left\{\sqrt{1.5^2 + 3^2}\right\} = \sqrt{\frac{9}{4} + 9} = \sqrt{\frac{9}{4} + \frac{36}{4}} = \sqrt{\frac{45}{4}} = \frac{3\sqrt{5}}{2}$
	<b>2.</b> $\left\{\sqrt{1.5^2 + 3^2}\right\} = \sqrt{11.25} = \sqrt{2.25}\sqrt{5} = 1.5\sqrt{5}$
(e)	M1: for an attempt at finding the area of either triangle <i>ABC</i> or triangle <i>ABE</i> .
	<b>B1:</b> Correct method for removing a square root. Eg: $\sqrt{80}\sqrt{5} = \sqrt{400} = 20$ or $\sqrt{5} \times 4\sqrt{5} = 20$
	Note: This mark can be implied.
	A1: for 45 only.
	<u>Alternative 1 to part (e):</u> Area $=\frac{1}{2}\left(\frac{3}{2}\sqrt{5}+3\sqrt{5}\right)\left(\sqrt{80}\right) = \frac{1}{2}(30+60) = 45$
	<b>M1:</b> $\frac{1}{2}(AB)(CE)$ . <b>B1:</b> Evidence of correct surd removal. <b>A1:</b> for 45.
	Note: Multiplying the diagonals (usually to find 90) is M0, B1 if surds are removed correctly, A0.
	<u>Alternative 2 to part (e):</u> Area = triangle DAC + triangle DCB + triangle DEA + triangle DBE
	$= \left(\frac{1}{2} \times \frac{3}{2}\sqrt{5} \times \sqrt{45}\right) + \left(\frac{1}{2} \times \frac{3}{2}\sqrt{5} \times \left(\sqrt{80} - \sqrt{45}\right)\right) + \left(\frac{1}{2} \times 3\sqrt{5} \times \sqrt{45}\right) + \left(\frac{1}{2} \times 3\sqrt{5} \times \left(\sqrt{80} - \sqrt{45}\right)\right)$
	$= \left(\frac{1}{2} \times \frac{3}{2}(15)\right) + \left(\frac{1}{2} \times \frac{3}{2}(5)\right) + \left(\frac{1}{2} \times 3(15)\right) + \left(\frac{1}{2} \times 3(5)\right)$
	$= \left(\frac{45}{4}\right) + \left(\frac{15}{4}\right) + \left(\frac{45}{2}\right) + \left(\frac{15}{2}\right)$
	= 45
	M1: For finding the area of one of the four triangles. B1: Evidence of correct surd removal. A1: for 45. <u>Alternative 3 to part (e):</u>
	$\left\{CE = CD + DE = \frac{3}{2}\sqrt{5} + 3\sqrt{5} = \frac{9}{2}\sqrt{5}\right\},  \left\{BD = DA + \underline{AB} = 3\sqrt{5} + \underline{4\sqrt{5}} = 7\sqrt{5}\right\}$
	Area = triangle $BCE$ - triangle $ACE = \frac{1}{2}(CE)(BD) - \frac{1}{2}(CE)(BD)$
	$= \frac{1}{2} \times \frac{9}{2} \sqrt{5} \times 7\sqrt{5} - \frac{1}{2} \times \frac{9}{2} \sqrt{5} \times 3\sqrt{5}$ M1: for an attempt at the area of triangle <i>BCE</i> or triangle <i>ACE</i> .
	$=\frac{63(5)}{4} - \frac{27(5)}{4} = \frac{36(5)}{4} = 9(5)$ B1: Evidence of correct surd removal.
	4   4   4 = 45
	A1. 101 43 0111y.

Question Number	Scheme	Mar	ks
<b>10.</b> (a)	{Coordinates of $A$ are} (4.5, 0) See notes below	B1	[1]
(b)(i)	у <b>—</b>		
	27 Horizontal translation	M1	
	-3 and their ft 1.5 on postitive <i>x</i> -axis	A1 ft	
	Maximum at 27 marked on the <i>y</i> -axis	B1	
	-3 $0$ $1.5$ x		[3]
(ii)	. y <b>≜</b>		[0]
	(1, 27) Correct shape, minimum at $(0, 0)$ and a	M1	
	maximum within the first quadrant. 1.5 on <i>x</i> -axis	A1 ft	
	Maximum at (1, 27)	B1	
	1.5		
	$C = \frac{1}{x}$		[3]
(c)	${k =} -17$	B1	[1] 8
$(\mathbf{a})$	<b>Notes</b>	1	
(a)	<b>B1:</b> For stating either $x = 4.5$ or $\frac{9}{2}$ or $\frac{18}{4}$ etc. or $A = 4.5$ or $\frac{9}{2}$ or $(4.5, 0)$ . Can be written on grap Allow $(0, 4.5)$ marked on curve for B1. Otherwise $(0, 4.5)$ without reference to any of the above		
(b)(i)	<b>M1:</b> for any horizontal (left-right) translation where minimum is still <b>on</b> $x$ -axis not at $(0, 0)$ .	C 18 D0.	
	Ignore any values.		
	A1ft: for -3 (NOT 3) and 1.5 (or their x in part (a) $-$ 3) <i>evaluated</i> and marked on the positive x-ax Allow (0, $-$ 3) and/or (0, ft 1.5) rather than ( $-3$ , 0) and (ft 1.5, 0) if marked in the		
	"correct" place on the x-axis. Note: Candidate <i>cannot</i> gain this mark if their x in part (a) $f$		an 3.
(ii)	<b>B1:</b> Maximum at 27 marked on the <i>y</i> -axis. <b>Note</b> : the maximum must be on the <i>y</i> -axis for this mar <b>M1:</b> for correct shape with minimum still at $(0, 0)$ and a maximum within the first quadrant. Igno		s.
	A1ft: for $\frac{\text{their } x \text{ in part } (a)}{3}$ ; as intercept on x-axis eg: $\frac{4.5}{3}$ or 1.5 or $\frac{3}{2}$ or $\frac{9}{6}$ Note: a generalised	$\frac{A}{3}$ is A	0.
	Allow $(0, \text{ ft } 1.5)$ rather than $(\text{ft } 1.5, 0)$ if marked in the "correct" place on the x-axis.	-	
	<b>B1:</b> Maximum at (1, 27) or allow 1 marked on the <i>x</i> -axis and the corresponding 27 marked on the <b>Note:</b> Be careful to look at the correct graph. The candidate may draw another graph to hel	-	'n
	answer part (c).	-	
	Note: You can recover (b)(i) $(-3, 0)$ and (ft 1.5, 0) or in (b)(ii) (ft 1.5, 0) as <i>correct coordinates</i> candidate's working if these are not marked on their sketch(es).	<i>only</i> in	
(c)	<b>B1:</b> for $(k = ) -17$ only. <b>BEWARE</b> : This could be written in the middle or at the bottom of a p	oage.	

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